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APPLICATION OF MATHEMATICAL MODELING IN ECOLOGY[4]

Abstract

The aim of this paper was implementation of mathematical modeling in ecological research on the example of the prevalence of odonates in Serbia. For research purposes cix areas were selected for which the number of species of odonants was given, a similarity coefficient was calculated, and based on the data as the number of species and environmental variables of the place (altitude, temperature and precipitation), multiple linear regression (MLR) model was presented describing the number of species odonants depending on altitude, temperature and precipitation. The areas studied were the rivers Tisa, Sava-Danube, Velika Morava, Južna Morava, as well as the mountain areas Zlatibor and Golija. The occurrence of the species was highest at the Sava-Danube site, followed by the Tisa. Odonates occurrence was lowest in the Golija site. The results of the study showed that environmental variables are significantly associated with odonates distribution. The MLR model based on the species dependence of altitude, temperature, and precipitation showed an extremely high degree of agreement.

Key words: Mathematical modeling, MLR, environmental factors

JEL classification: C0, C1,Q54

ПРИМЕНА МАТЕМАТИЧКОГ МОДЕЛОВАЊА У ЕКОЛОГИЈИ

Апстракт

Циљ рада је примена математичког моделирања у еколошким истраживањима на примеру распрострањености одонаната у Србији. За потребе истраживања

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одабрано је шест подручја за која је дат број врста одонаната, затим је израчунат коефицијент сличности а на основу података о броју врста и чинилаца спољашње средине (надморска висина, температура и падавине), док је моделом вишеструке линеарне регресије (МЛР) представљен број врста одонаната врста у зависности од надморске висине, температуре и падавина. Проучавана подручја били су речни токови Тисе, Сава-Дунав, Велике Мораве, Јужне Мораве, као и планинска подручја Златибора и Голије. Број врста био је највећи на месту Сава-Дунав, а затим на подручју Тисе. Појава одоната била је најмања на подручју места Голије. Резултати истраживања су показали да су променљиви чиниоци животне средине значајно повезани са дистрибуцијом одоната. Модел МЛР заснован на зависностима од висине, температуре и падавина показао је изузетно висок степен слагања.

Кључне речи: *Математичко моделовање, MLR, еколошки чиниоци*

Introduction

In the field of ecology, scientists are confronted with the dynamics of nature, in terms of population growth or decline in a large number of plant and animal species. Given the strong influence of man and nature and the entire living world, it is necessary to apply mathematical models that will evaluate the impact of the environment on a population of some species. Knowledge about the environmental impact on living organisms may contribute to their preservation (Suhling et al., 2006).

Species are not similarly distributed across the Earth. The serious decrease in species number (Chapin et al. 2000) increased the urgency to understand species distribution in order to develop effective conservation strategies (Robinet et al. 2019; Franzese et al. 2019). An understanding of the relationship between species and the environment is of great importance (Williams et al., 2002).

The utilization of insect as bioindicators is limited to their habitat type (McGeoch, 1998). The odonates are freshwater invertebrates and are often used as ecological indicators of habitat quality (Hardersen, 2000; Sahlen and Ekestubbe, 2001; Silva et al., 2010; Arimoro et al., 2011; Simaika and Samways, 2011). Some studies (Samways and Steytler, 1996; Oppel, 2006; Silva et al., 2010) have pointed out that odonates may serve as an indicator for changes in landscapes. But, their reaction to environmental conditions in numerous areas of the world is unknown (Bried and Mazzacano, 2010; Clausnitzer et al., 2012). Knowledge about the environmental impact on odonates may contribute to their preservation (Sahlen and Ekestubbe, 2001; Suhling et al., 2006).

A substantial number of studies have focused on the impact of temperature and precipitation on distribution odonata (Hickling et al., 2005; Finch et al., 2006; Hassall, 2012). Temperature increments may encourage the development of odonata species ranges and lead to increments in local biodiversity in northern latitudes (Hassall and Thompson, 2008).

Latitudinal gradients in species richness are observed for a wide range of taxonomic groups (Gaston 2000). Spatial patterns in species richness can be described as the result of several mechanisms (Gaston and Blackburn 1990). Among the factors crucial for the

impact on the species number of some area, the most dominant are: altitude (Rahbek 1995), energy availability (Gaston 2000), climate (Rohde, 1992), habitat heterogeneity (Rahbek and Graves 2000; Kerr 2001), and disturbance (Huston 1994).

No previous studies have addressed the effects of climate and habitat parameters on odonates in Serbia. In this study, factors that influence number of species in Serbia were examined. The effects of temperature, precipitation and altitude on the number of odonates species were investigated. So, the potential of odonates to serve as indicators of climate effects on freshwater systems of this region was evaluated.

Materials and methods

Serbia is situated in the Danube basin on the edge of the Mediterranean area, covering 88,361 km^2 (Fig. 1). Serbia has rich genetic, species, and ecosystem diversity because of its geographic position (continental and Mediterranean influences, relief...). (Amidžić et al., 2014)

The paper analyzes the biodiversity of the odontas, both on the territory of the whole Republic of Serbia and at 6 different specific sites (Đukić, 2014). Collected data are average temperature, altitudes, and precipitation of regions from Republic Hydrometeorological Service of Serbia, Figures 2, 3 and 4.

The first site (1) is located in the north of Serbia, and this is the stream of the Tisa River. This site can be characterized by an altitude of up to 200m, mean annual temperatures around 15-25 °C, and precipitation (up to 600 mm per year). The second site (2) is a part of the stream and the mouth of the Sava and Danube rivers around Belgrade. The altitude is 400 m in this area. The mean annual temperature ranges from 20-25 °C. Precipitation is 600-700 mm. The third site (3) is the stream of the Velika Morava, at an altitude of 400 m. The mean annual temperature ranges from 10-15 °C. Precipitation is 600-700 mm. Zlatibor is the fourth selected site (4) in the southeastern part of Serbia. This site has a significantly higher altitude, up to 1500m, mean annual temperature 10-15 °C, and precipitation level 800-900 mm per year. The fifth site is the stream of the Južna Morava river (5), at an altitude of 400 m, the mean annual temperature is 5-10 °C, and the level of precipitation is 900-1000 mm per year. The last site is mount Golija (6), altitude above 1600 m, mean annual temperature 10-15 °C, and precipitation level up to 600 mm.

Figure 1: Study area map

Source: Google maps and Alciphron - database of insects in Serbia (Odonata)

Data analysis. The Jaccard coefficient of similarity (Jt) determines the similarity of the fauna of the investigated sites and is calculated as

$$J_t = \frac{m_{11}}{(m_{11} + m_{10} + m_{01})}$$

t – fauna of areas we compare, m_{11} - number of species common to both fauna we compare, m_{10} - number of species present in the first of the comparing fauna, m_{01} - number of species present in another fauna.

MLR model in Statistica. Multiple linear regression analyses are widely used in the analysis of data in ecology. It is widely used because it results in an equation that contains the effects of all variables that we want to consider in the description of a phenomenon or process (Boldina and Beninger 2016).

Results and discussion

The number of species registered by sites are as follows: S1= 42, S2= 49, S3=33, S4= 32, S5= 39, S6= 13. Table 1 shows coefficient of similarity among observed sites in the form of a matrix.

Table 1. Jacarrd´s coefficient between sites

J_r	1	2	3	4	5	6
1	1	0.70	0.46	0.48	0.56	0.15
2		1	0.61	0.57	0.74	0.20
3			1	0.57	0.66	0.15

					1	0.78	0.22
4					1	0.78	0.22
5						1	0.21
6							1

Source: Alciphron - database of insects in Serbia (Odonata) and RHS

The data required for model formation (MLR) are given in Table 2. Survey data indicate that the largest number of species has been identified in the S2 area, at an altitude of 400 m, with an average annual temperature of 22.5 °C and an annual rainfall of 700 mm. On the other hand, the smallest number of species is identified in the S6 area, with an altitude of 1800 m and an average annual temperature of 12.5 °C.

Table 2 Number of species by region and basic environmental parameters

Region	S	H (m)	t (°C)	p (mm)
1	42	200	20	600
2	48	400	22.5	700
3	34	400	12.5	700
4	32	1500	12.5	900
5	39	400	7.5	1000
6	13	1800	12.5	600

Source: Alciphron - database of insects in Serbia (Odonata) and RHS

Correlation coefficients between altitude (h), temperature (t) and precipitation (prec.) are:
$r (h - t) = - 0.33$ $r (h - p) = - 0.03$ $r (t - p) = - 0.63$

According the results, species occurrence was highest in Sava-Dunav site, followed by Tisa site. Odonates occurrence was lowest in the Golija site. In order to express the similarity of the fauna of the explored sites, the Jaccard coefficient was used and a high percentage of similarities was found among most of sites, with the exception of Golija. Based on the calculated correlations, Table 3, the inverse proportionality between the number of species and altitudes is found as the most dominant.

The resulting MLR model is shown in Table 3. The equation is given as follows:
$S (h, t, per.) = \beta_0 + \beta_1 \cdot h + \beta_2 \cdot t + \beta_3 \cdot prec.$

Table 3: MLR model of species number in dependence of altitude, temperature and precipitation

	Beta	St.err. of Beta	B	St.err. of B	t (2)	p-level
Interception			-15.433	5.1553	-2.993	0.0958
h	-0.5917	0.0488	-0.010	0.0009	-12.114	0.0067
t	0.7097	0.0627	1.536	0.1358	11.309	0.0077
prec.	0.6519	0.0592	0.048	0.0043	11.005	0.0081

Source: Alciphron - database of insects in Serbia (Odonata) and RHS

$R=0.99809045$ $R^2=0.99618454$ $adj.R^2=0.99046135$
$F_{(3, 2)}=174.06$ $p<0.00572$ St.err.of estim.$=1.1779$

Based on the MLR, Table 3, temperature is found as the most dominant factor that influence odonates diversity (the highest B value).

Conclusion

Based on the results presented in the paper, it is possible to conclude the great importance of temperature on the diversity of the odonata in six observed sites. Increasing the number of species corresponds to the environment with higher temperature and lower altitude. The highest number of odonates species is found along the river flows in the plain area, while the smallest number of speciesis found on the mountainous areas. The MLR model shows the dependence of the number of species in some area, of an altitude, temperature and precipitation. The resulting model shows a high level of agreement with real values, R> 0.99.

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